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4.

$$q(t) = 1*(t) \quad q(t) = A*\text{Sin } \omega t,$$

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$$\omega = 2c^{-1}.$$

II.

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W (p).

W (p),

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4.

$$W_{\Delta x}(p) = 1 - W(p) = \frac{1}{1 + W_{pa}(p)}$$

$$q(t) = 1^*(t):$$

$$\Delta X_{YCT} = \lim_{p \rightarrow 0} p W_{\Delta x}(p) * X(p)$$

$$q(t) = 1^*(t)$$

$$X(p) = \frac{1}{p}$$

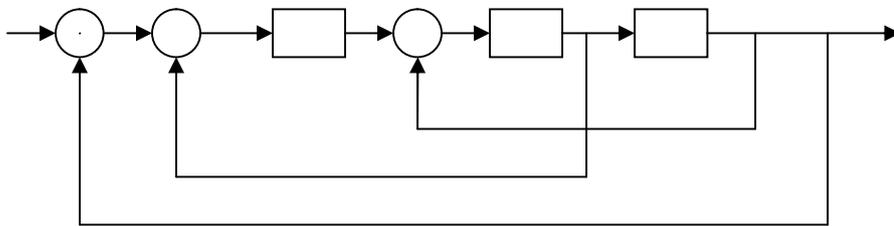
$$q(t) = A * \sin \omega t$$

:

$$X_{\max} \approx \frac{A}{A(\omega_k)}$$

III.

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$$T_2^2 \frac{d^2 y}{dt^2} + T_1 \frac{dy}{dt} + y = k \cdot x$$

$$k = 5.0; T_1 = 1.0; T_2 = 0.05$$

:

$$T_1 \frac{dY}{dt} + Y = T_2 \frac{dX}{dt} + K \cdot X$$

$$K = 10; T_1 = 1.0; T_2 = 15$$

:

$$T_1 \frac{dY}{dt} + Y = K \cdot X$$

$$K = 1.5; T = 0.5$$

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$$W_1(p) = \frac{k}{T_2^2 p^2 + T_1 p + 1} = \frac{5}{(0.05)^2 p^2 + 1 p + 1}$$

1.2.

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$$W_2(p) = \frac{K + T_2 p}{T_1 p + 1} = \frac{10 + 15 p}{1 + p}$$

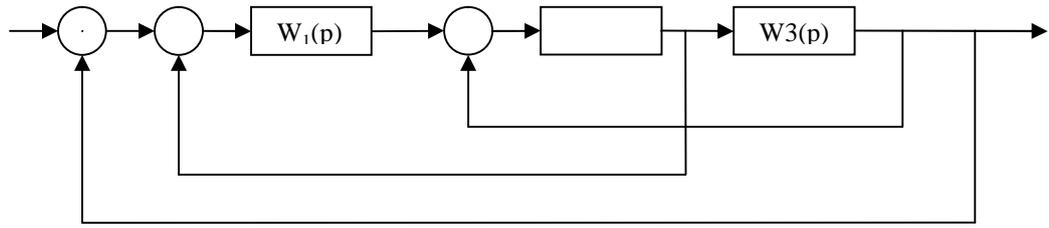
1.3.

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$$W_3(p) = \frac{K}{T p + 1} = \frac{1.5}{0.5 p + 1}$$

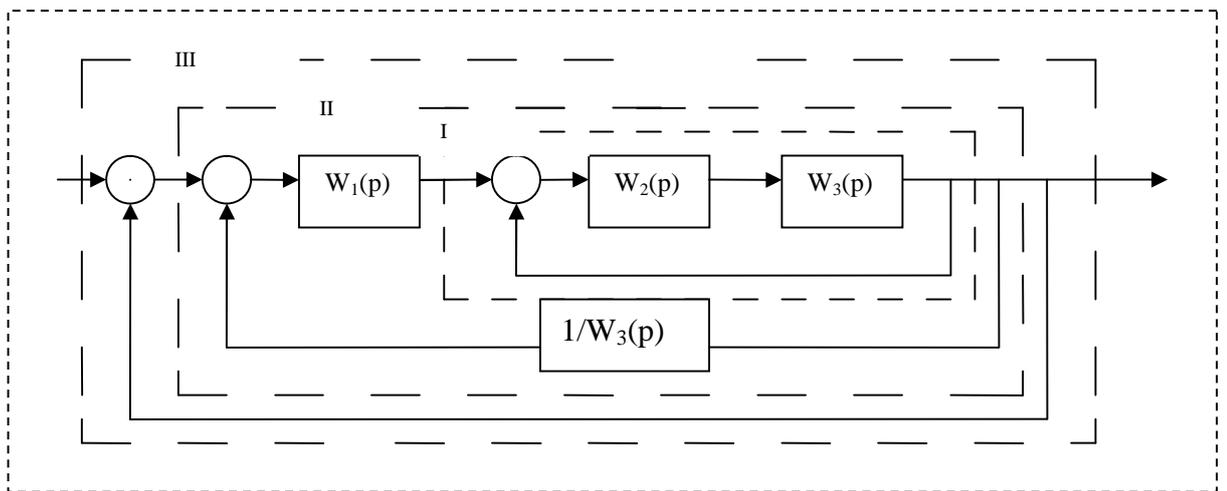
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$$W_{1k}(p) = \frac{W_2(p)W_3(p)}{1 + W_2(p)W_3(p)}$$

2- :

$$W_{lk}(p) = \frac{W_{lk}(p)W_1(p)}{1 + W_{lk}(p)W_1(p) \frac{1}{W_3(p)}} = \frac{W_1(p)W_2(p)W_3(p)}{1 + W_2(p)W_3(p) + W_1(p)W_2(p)}$$

3.

$$\begin{aligned}
W(p) = W_{\text{III}}(p) &= \frac{W_1(p)W_2(p)W_3(p)}{1+W_2(p)W_3(p)+W_1(p)W_2(p)} = \\
&= \frac{\frac{5}{(0.05)^2 p^2 + p + 1} * \frac{10+15p}{1+p} * \frac{1.5}{0.5p+1}}{1 + \frac{10+15p}{1+p} * \frac{1.5}{0.5p+1} + \frac{5}{(0.05)^2 p^2 + p + 1} * \frac{10+15p}{1+p}} = \\
&= \frac{75+112.5p}{0.00125p^4 + 0.56p^3 + 36.1p^2 + 110p + 127} = \frac{K+112.5p}{0.00125p^4 + 0.56p^3 + 36.1p^2 + 110p + 127}. \quad (1)
\end{aligned}$$

:

$$W(p) = \frac{W_{pa3}(p)}{1+W_{pa3}(p)} \quad (2)$$

,

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$$\begin{aligned}
W(p) &= \frac{K+112,5p}{0,00125p^4 + 0.56p^3 + 36.1p^2 + 222.5p + (K+127)} = \\
&= \frac{75+112,5p}{0,00125p^4 + 0.56p^3 + 36.1p^2 + 222.5p + 202}; \quad (3)
\end{aligned}$$

$$0,00125p^4 + 0,56p^3 + 36,1p^2 + 222.5p + 202 = 0. \quad (4)$$

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$$\Delta_4 = \begin{vmatrix} 0.56 & 222.5 & 0 & 0 \\ 0.00125 & 36.1 & 202 & 0 \\ 0 & 0.56 & 222.5 & 0 \\ 0 & 0.00125 & 36.1 & 202 \end{vmatrix}$$

2-

$$\Delta_2 = 0.56 * 36.1 - 222.5 * 0.00125 \approx 19.9 > 0$$

3-

$$\Delta_3 = 222.5 * \Delta_2 - 0.56(0.56 * 202 - 0.00125 * 0) \approx 4364 -$$

$$\Delta_3 = 0$$

$$\begin{array}{ccc} 0.56 & 222.5 & 0 \\ 0.00125 & 36.1 & (K + 127) \\ 0 & 0.56 & 222.5 \end{array} = 0$$

$$0.00125p^4 + 0.56p^3 + 36.1p^2 + 222.5p + (K + 127) = 0 \quad (5)$$

3-

$$222,5 * \Delta_2 - (K + 127)(0,56 * 0,56 - 222,5 * 0) = 0$$

$$= \frac{4369}{0.3136} \approx 14019$$

$$= 14019$$

3.

$$(4) p = j\omega :$$

$$0.00125(j\omega)^4 + 0.56(j\omega)^3 + 36.1(j\omega)^2 + 222.5(j\omega) + 202 = 0 \quad (6)$$

$$j = \sqrt{-1}; \quad j^2 = -1; \quad j^3 = -j; \quad j^4 = 1$$

(6):

$$\text{Re}(\omega) = 0.00125 \omega^4 - 36.1 \omega^2 + 202;$$

$$\text{Im}(\omega) = -0.56 \omega^3 + 222.5 \omega.$$

$$0 \leq \omega < \infty ,$$

$$\text{Re}(\omega) \quad \text{Im}(\omega).$$

3

3.

ω	0	1	2	3	5	10	100	500	∞
$\text{Re}(\omega)$	202	166	58	-123	-700	-3395			
$\text{Im}(\omega)$	0	222	441	655	153	1665			

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$$\omega_1 < \omega_2 < \omega_3 < \omega_4,$$

$$\omega_1, \omega_2, \omega_3, \omega_4$$

:

$$\begin{cases} 0.00125\omega^4 - 36.1\omega^2 + 202 = 0 \\ -0.56\omega^3 + 222.5\omega = 0 \end{cases}$$

:

$$\omega_2 = 2.8 ; \omega_4 = 170$$

:

$$\omega_1 = 0 ; \omega_3 = 19.93$$

$$\omega_1 < \omega_2 < \omega_3 < \omega_4, . . .$$

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$$\text{Im}(\omega) = 0; \text{Re}(\omega) = 0,$$

$\omega \neq 0.$

$$(5) \quad p = j \omega$$

$$D(j\omega) = \text{Re}(\omega) + j\text{Im}(\omega)$$

$$\begin{cases} \text{Re}(\omega) = 0.00125\omega^4 - 36.1\omega^2 + (K_p + 127) \\ \text{Im}(\omega) = -0.56\omega^3 + 222.5\omega = 0 \end{cases}$$

$$\text{Re}(\omega) = 0$$

$$= 14019$$

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4.

$$W_{\Delta x}(p) = 1 - W_{3am}(p) = 1 - \frac{75 + 112.5p}{0.00125p^4 + 0.56p^3 + 36.1p^2 + 222.5p + 202}$$

$$X(p) = 1/p, \quad q(t) = 1(t)$$

$$\Delta X_{yct} = \lim_{p \rightarrow 0} p W_{\Delta x}(p) X(p) = \lim_{p \rightarrow 0} p^* \frac{1}{p} \left[1 - \frac{75 + 112.5p}{0.00125p^4 + 0.56p^3 + 36.1p^2 + 222.5p + 202} \right] = 0.63$$

$$(1) p = j \omega:$$

$$W(j\omega) = \frac{75 + 112.5(j\omega)}{0.00125(j\omega)^4 + 0.56(j\omega)^3 + 36.1(j\omega)^2 + 110.0(j\omega) + 127} \quad (7)$$

$$A(\omega) = |W_{pa3}(j\omega)| = \sqrt{[\text{Re}(\omega)]^2 + [\text{Im}(\omega)]^2} \quad (8)$$

Re Im -

- (7), :

$$W(j\omega) = \text{Re}(\omega) + j\text{Im}(\omega)$$

(7)

$$W(j\omega) = \frac{75(0.00125\omega^4 - 36.1\omega^2 + 127) + 112.5\omega(110\omega - 0.56\omega^3)}{(0.00125\omega^4 - 36.1\omega^2 + 127) + (110\omega - 0.56\omega^3)^2} - j \frac{75(110\omega - 0.56\omega^3) + 112.5\omega(0.00125\omega^4 - 36.1\omega^2 + 127)}{(0.00125\omega^4 - 36.1\omega^2 + 127) + (110\omega - 0.56\omega^3)^2} \quad (9)$$

(9) (8) :

$$A(\omega) = |W_{pa3}(j\omega)| = \sqrt{\frac{5625 + 12656.25\omega^2}{(0.00125\omega^4 - 36.1\omega^2 + 127)^2 + (110\omega - 0.56\omega^3)^2}} \quad (10)$$

,

$$X_{\max} \approx \frac{A}{|W_{pa3}(j\omega_k)|}$$

=10 -

; ω_k -

$$; |W_{pa3}(j\omega_k)| = A(\omega_k) -$$

$$\omega = \omega_k = 2$$

$$X_{\max} = \frac{10}{\sqrt{\frac{5625 + 12656.25(2)^2}{[(0.00125(2)^4 - 36.1(2)^2 + 127]^2 + [110*2 - 0.56(2)^3]^2}}} = \frac{10}{\sqrt{1.11}} \approx 9.5$$

IV.

1.

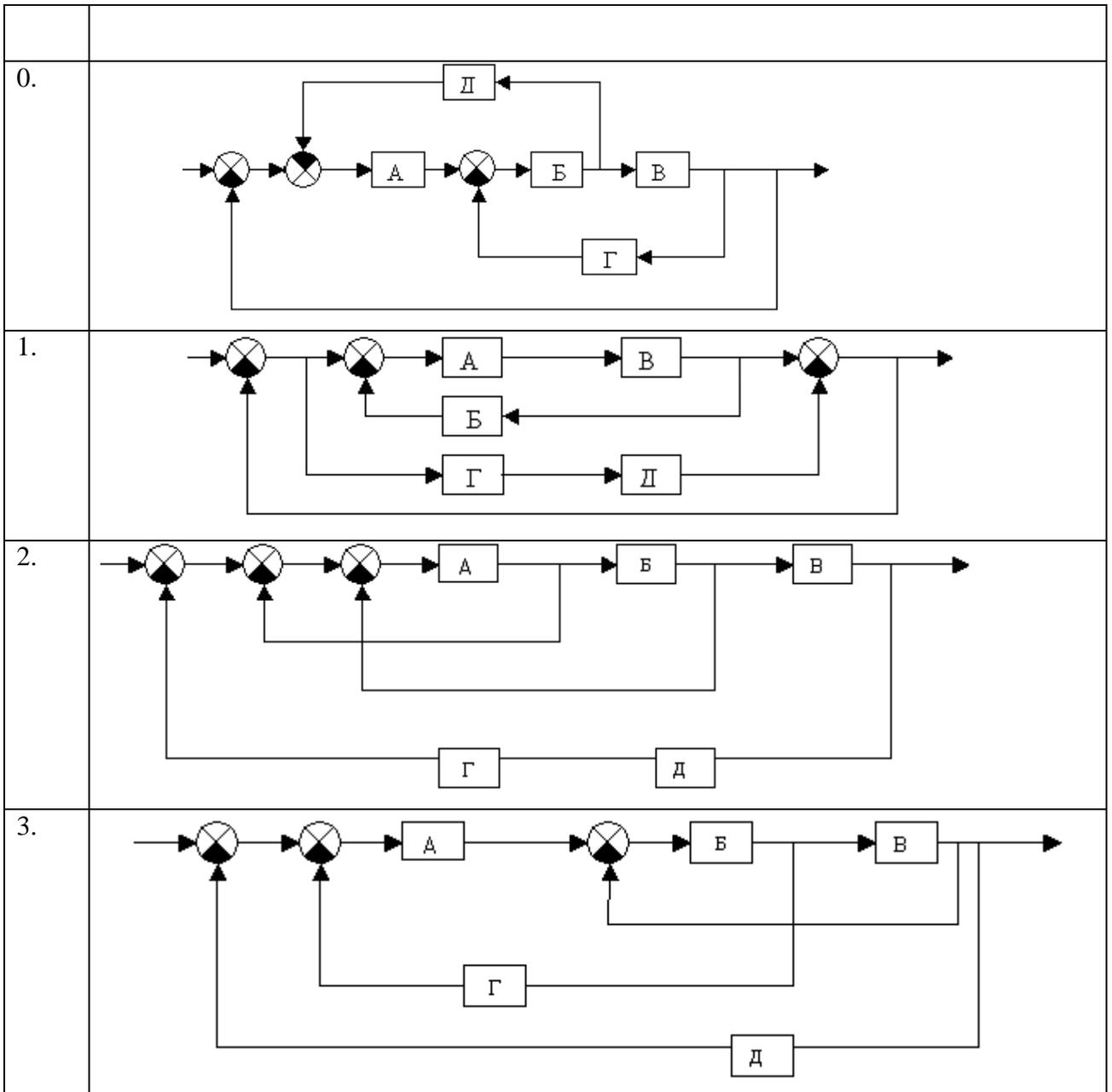
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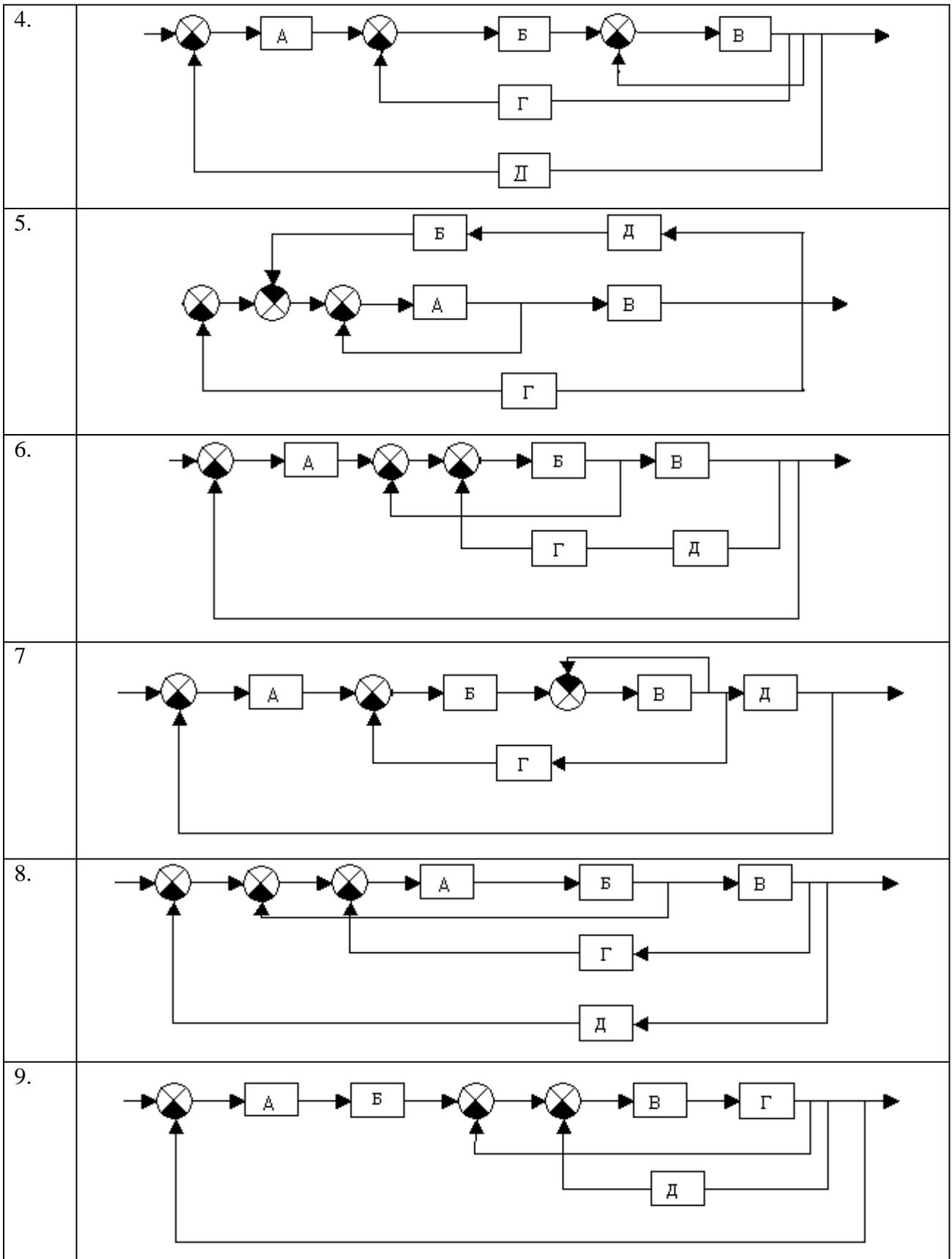
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1	2	3	4
0		${}_1 \frac{dY}{dt} + Y = K \quad {}_2 \frac{dX}{dt}$ $\frac{dY}{dt} + Y = K^*$ $\frac{dY}{dt} = K^*$ $Y = K^*$ $\frac{dY}{dt} + Y = K^*$	<p>K=3; T₁=1; T₂=0,5</p> <p>K=1; T=1</p> <p>K=6; T=0,3</p> <p>K=3</p> <p>K=5; T=0,5</p>
1		$T_2^2 \frac{d^2 Y}{dt^2} + {}_1 \frac{dY}{dt} + Y = K^* X$ ${}_1 \frac{dY}{dt} + Y = K^* \quad {}_2 \frac{dX}{dt}$ ${}_1 \frac{dY}{dt} + Y = K^* \quad {}_2 \frac{dX}{dt} + K^* X$ $Y = K^*$ $Y = K^*$	<p>K=1; T₁=0,2; T₂²=0,02</p> <p>K=3; T₁=1; T₂=2</p> <p>K=2; T₁=1; T₂=0.5</p> <p>K=6</p> <p>K=0.5</p>
2		$T_2^2 \frac{d^2 Y}{dt^2} + {}_1 \frac{dY}{dt} + Y = K^* X$ $\frac{dY}{dt} + Y = K^*$ $\frac{dY}{dt} = K^*$ $Y = K^*$ $T^* Y = K \frac{dX}{dt}$	<p>K=0.5; T₁=0.2; T₂²=0.1</p> <p>K=10; T=1</p> <p>K=1; T=0.2</p> <p>K=4</p> <p>K=1; T=0.3</p>

3		$T_2^2 \frac{d^2 Y}{dt^2} + Y = K^*$ $Y = K^* X$ ${}_2 \frac{dY}{dt} + Y = K^* \quad {}_1 \frac{dX}{dt} + K^* X$ $Y = K^*$ $\frac{dY}{dt} + Y = K^*$	$K=4; T_2^2=0.6$ $K=2$ $K=4; T_1=0.5; T_2=1.5$ $K=7$ $K=3; T=0.4$
4		$\frac{dY}{dt} + Y = K^*$ $\frac{dY}{dt} + Y = K^*$ $\frac{dY}{dt} = K^*$ $Y = K^*$ ${}_2 \frac{dY}{dt} + Y = K^* \quad {}_1 \frac{dX}{dt} + K^* X$	$K=5; T=0.5$ $K=1; T=0.8$ $K=2; T=1.0$ $K=9$ $K=0.5; T_1=0.2; T_2=0.5$
5		$T_2^2 \frac{d^2 Y}{dt^2} + {}_1 \frac{dY}{dt} + Y = K^* X$ $\frac{dY}{dt} = K^*$ $T^* Y = K^* \frac{dX}{dt}$ $Y = K^*$ $\frac{dY}{dt} + Y = K^*$	$K=2; T_1=0.3; T_2^2=0.14$ $K=5; T=2$ $K=1; T=0.5$ $K=10$ $K=4; T=1$
6		$\frac{dY}{dt} + Y = K^*$ $T_2^2 \frac{d^2 Y}{dt^2} + {}_1 \frac{dY}{dt} + Y = K^* X$ ${}_2 \frac{dY}{dt} + Y = K^* \quad {}_1 \frac{dX}{dt} + K^* X$ $Y = K^*$	$K=1; T=0.2$ $K=2; T_2^2=0.12$ $K=3; T_1=0.5; T_2=1$ $K=0.5$

		$Y = K^*$	$K=0.5$
7		$T_2^2 \frac{d^2 Y}{dt^2} + {}_1 \frac{dY}{dt} + Y = K^* X$ $T^* Y = K^* \frac{dX}{dt}$ ${}_2 \frac{dY}{dt} + Y = K^* {}_1 \frac{dX}{dt} + K^* X$ $Y = K^*$ $Y = K^*$	$K=0.3; T_1=3; T_2^2=0.05$ $K=0.5; T=1$ $K=4; T_1=0.5; T_2=1$ $K=6$ $K=1$
8		$T_2^2 \frac{d^2 Y}{dt^2} + {}_1 \frac{dY}{dt} + Y = K^* X$ $\frac{dY}{dt} + Y = K^*$ $\frac{dY}{dt} = K^*$ $Y = K^*$ $*Y = K^* \frac{dX}{dt}$	$K=2; T_1=3; T_2^2=0.12$ $K=8; T=1$ $K=5; T=0.2$ $K=12$ $K=2; T=0.3$
9		$T_2^2 \frac{d^2 Y}{dt^2} + Y = K^* X$ $\frac{dY}{dt} + Y = K^*$ ${}_2 \frac{dY}{dt} + Y = K^* {}_1 \frac{dX}{dt} + K^* X$ $Y = K^*$ ${}_1 *Y = K^* \frac{dX}{dt}$	$K=2; T_2^2=0.2$ $K=5; T=1.2$ $K=2.5; T_1=0.5; T_2=1$ $K=1$ $K=2.5; T_1=1$

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- ., « », 1990., 367 .
2.
- , « », 1987., 398 .

$$\begin{array}{r}
 \underline{1,2} \dots, \quad 60 \quad \frac{84 \frac{1}{16}}{10} \quad 20 \quad . \\
 - \quad \quad \quad 39. \quad .
 \end{array}$$