

O`zbekiston Oliy va o`rta maxsus ta`lim vazirligi

Namangan Davlat universiteti

Fizika-matematika fakul'teti *«Matematika» kafedrası*

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Oliy ta`limning 5130100-Matematika yo`nalishi I-bosqich
talabalari kunduzgi bo`limi uchun

«Matematik tahlil»
fanidan

«**Sonli ketma-ketlik va uning limiti**»
mavzusi bo`yicha

amaliy dars ishlanmasi

Mazkur amaliy dars ishlanmasida sonli ketma-ketlik, chegaralangan sonli ketma-ketlik, nuqtaning atrofi, sonli ketma-ketlikning limiti tushunchalari bayon qilingan. Dars amaliy mashg`ulot bo`lgani sababli, ishchi dasturda ko`rsatilgan adabiyotlar bo`yicha ko`pgina misollar oddiydan murakkablashtirilib ishlab ko`rsatilgan va mavzuga oid test savollari, mustaqil ish topshiriqlari va adabiyotlar ro`yxati keltirilgan

Namangan-2011

MAVZU. Sonli ketma-ketlik va uning limiti.

REJA:

1. Sonlar ketma-ketligi tushunchasi.
2. Sonlar ketma-ketligining limiti.
3. Mavzuga doir misollar.
4. Mavzuga doir testlar.
5. Mustaqil ish topshiriqlari.

1. Sonlar ketma-ketligi tushunchasi.

Har bir natural n songa biror haqiqiy x_n sonini mos qo'yuvchi

$$f : n \rightarrow x_n, \quad (n = 1, 2, 3, \dots) \quad (1)$$

akslantirishni qaraymiz.

1-ta'rif. 1- akslantirishning akslaridan iborat ushbu

$$x_1, x_2, x_3, \dots, x_n, \dots \quad (2)$$

to'plam **sonlar ketma-ketligi** deyiladi. Uni $\{x_n\}$ yoki x_n kabi belgilanadi.

x_n ($n = 1, 2, 3, \dots$) sonlar (2) **ketma-ketlikning hadlari** deyiladi. Masalan,

$$1) x_n = \frac{1}{n} : 1, \frac{1}{2}, \frac{1}{3}, \dots, \frac{1}{n}, \dots,$$

$$2) x_n = (-1)^n : -1, 1, -1, \dots, (-1)^n, \dots$$

$$3) x_n = \sqrt[n]{n} : 1, \sqrt{2}, \sqrt[3]{3}, \dots, \sqrt[n]{n}, \dots$$

$$4) x_n = 1 : 1, 1, 1, \dots, 1, \dots$$

$$5) 0,3; 0,33; 0,333; \dots; 0, \underbrace{333 \dots 3}_{n \text{ ta}}; \dots$$

lar sonlar ketma-ketliklaridir.

Biror $\{x_n\}$ ketma-ketlik berilgan bo'lsin.

2-ta'rif. Agar shunday o'zgarmas M soni mavjud bo'lsaki, ixtiyoriy x_n ($n = 1, 2, 3, \dots$) uchun $x_n \leq M$ tengsizlik bajarilsa (ya'ni $\exists M, \forall n \in N : x_n \leq M$ bo'lsa), $\{x_n\}$ ketma-ketlik **yuqoridan chegaralangan** deyiladi.

3-ta'rif. Agar shunday o'zgarmas m soni mavjud bo'lsaki, ixtiyoriy x_n ($n = 1, 2, 3, \dots$) uchun $x_n \geq m$ tengsizlik bajarilsa (ya'ni, $\exists m, \forall n \in N : x_n \geq m$ bo'lsa), $\{x_n\}$ ketma-ketlik **quyidan chegaralangan** deyiladi.

4-ta'rif. Agar $\{x_n\}$ ketma-ketlik ham yuqoridan, ham quyidan chegaralangan bo'lsa (ya'ni $\exists m, M, \forall n \in N : m \leq x_n \leq M$ bo'lsa), $\{x_n\}$ ketma-ketlik **chegaralangan** deyiladi. **Misol.** Ushbu

$$x_n = \frac{n}{4 + n^2} \quad (n = 1, 2, 3, \dots)$$

ketma-ketlikning chegaralanganligi isbotlansin.

◀ Ravshanki, $\forall n \in N$ uchun

$$x_n = \frac{n}{4 + n^2} > 0$$

bo'ladi. Demak, qaralayotgan ketma-ketlik quyidan chegaralangan.

Ma'lumki,

$$0 \leq (n - 2)^2 = n^2 - 4n + 4$$

bo`lib, undan $4n \leq 4 + n^2$ ya`ni,

$$\frac{n}{4 + n^2} \leq \frac{1}{4}$$

bo`lishi kelib chiqadi. Bu esa berilgan ketma-ketlikning yuqoridan chegaralanganligini bildiradi. Demak, ketma-ketlik chegaralangan ►

5-ta`rif. Agar $\{x_n\}$ ketma-ketlik uchun

$$\forall M \in R, \exists n_0 \in N : x_{n_0} > M$$

bo`lsa, **ketma-ketlik yuqoridan chegaralanmagan** deyiladi.

2. Sonlar ketma-ketligining limiti.

Aytaylik, $a \in R$ son hamda ixtiyoriy musbat ε son berilgan bo`lsin.

6-ta`rif. Ushbu

$$U_\varepsilon(a) = \{x \in R \mid a - \varepsilon < x < a + \varepsilon\} = (a - \varepsilon, a + \varepsilon)$$

to`plam a **nuqtaning ε - atrofi** deyiladi.

Faraz qilaylik $\{x_n\}$ ketma-ketlik va $a \in R$ soni berilgan bo`lsin.

7-ta`rif. Agar ixtiyoriy $\varepsilon > 0$ son olinganda ham shunday n_0 natural soni mavjud bo`lsaki, $n > n_0$ tengsizlikni qanoatlantiruvchi barcha natural sonlar uchun

$$|x_n - a| < \varepsilon \quad (3)$$

tengsizlik bajarilsa, (ya`ni

$$\forall \varepsilon > 0, \exists n_0 \in N, \forall n > n_0 : |x_n - a| < \varepsilon$$

bo`lsa), a son $\{x_n\}$ **ketma-ketlikning limiti** deyiladi va

$$a = \lim_{n \rightarrow \infty} x_n \text{ yoki } n \rightarrow \infty \text{ da } x_n \rightarrow a$$

kabi belgilanadi.

Ravshanki, yuqoridagi (3) tengsizlik uchun

$$|x_n - a| < \varepsilon \Leftrightarrow a - \varepsilon < x_n < a + \varepsilon$$

ya`ni, $x_n \in U_\varepsilon(a)$, ($n > n_0$) bo`ladi. SHuni e`tiborga olib, ketma-ketlikning limitini quyidagicha ta`riflasha bo`ladi.

8-ta`rif. Agar a nuqtaning ixtiyoriy $U_\varepsilon(a)$ atrofi olinganda ham $\{x_n\}$ ketma-ketlikning biror hadidan keyingi barcha hadlari shu atrofga tegishli bo`lsa, a son $\{x_n\}$ ketma-ketlikning limiti deyiladi.

Yuqorida keltirilgan ta`riflardan ko`rinadiki ε ixtiyoriy musbat son bo`lib, natural n_0 soni esa ε ga va qaralayotgan ketma-ketlikka bog`liq ravishda topiladi.

Misol. Ushbu

$$x_n = c \quad (c \in R, n = 1, 2, 3, \dots)$$

ketma-ketlikning limiti c ga teng bo`ladi.

◀Haqiqatan ham, bu holda $\forall \varepsilon > 0$ ga ko`ra $n_0 = 1$ deyilsa, unda $\forall n > n_0$ uchun $|x_n - c| = 0 < \varepsilon$ bo`ladi. Demak, $\lim_{n \rightarrow \infty} x_n = \lim_{n \rightarrow \infty} c = c$ ►

Teorema. Agar $\{x_n\}$ ketma-ketlik limitga ega bo`lsa, u yagona bo`ladi.

3. Mavzuga doir misollar.

41. Ketma-ketlik limitining ta'rifidan foydalanib $x_n = \frac{n}{n+1}$, $n = 1, 2, \dots$ ketma-ketlik uchun

$\lim_{n \rightarrow \infty} x_n = 1$ ekanini isbotlang, ya'ni ixtiyoriy $\varepsilon > 0$ uchun $n > N$ bo'lganda $|x_n - 1| < \varepsilon$ tengsizlik bajariladigan $N(\varepsilon)$ sonni toping.

Quyidagi jadvalni to'ldiring:

ε	0,1	0,01	0,001	0,0001
N				

◀ Ketma-ketlik limitining ta'rifiga ko'ra ixtiyoriy $\varepsilon > 0$ uchun

$$\left| \frac{n}{n+1} - 1 \right| = \left| \frac{-1}{n+1} \right| = \frac{1}{n+1} < \varepsilon$$

ga egamiz. Bu tengsizlikni n ga nisbatan echib $N(\varepsilon)$ ni topamiz:

$$n > \frac{1}{\varepsilon} - 1 \Rightarrow N(\varepsilon) = \left[\frac{1}{\varepsilon} - 1 \right].$$

Jadvalni to'ldiramiz:

ε	0,1	0,01	0,001	0,0001
N	9	99	999	9999



42. x_n ($n = 1, 2, \dots$) ketma-ketlik cheksiz kichik ($\lim_{n \rightarrow \infty} x_n = 0$) ekanini isbotlang, ya'ni ixtiyoriy $\varepsilon > 0$ uchun $n > N$ bo'lganda $|x_n| < \varepsilon$ tengsizlik bajariladigan $N(\varepsilon)$ sonni ko'rsating.

a) $x_n = \frac{(-1)^{n+1}}{n}$; b) $x_n = \frac{2n}{n^3 + 1}$; e) $x_n = \frac{1}{n!}$; z) $x_n = (-1)^n \cdot 0,999^n$.

◀ Ketma-ketlik limitining ta'rifidan foydalanamiz. Ixtiyoriy $\varepsilon > 0$ uchun

b) $\left| \frac{2n}{n^3 + 1} \right| < \frac{2n}{n^3} = \frac{2}{n^2} < \varepsilon \Leftrightarrow n < \sqrt{\frac{2}{\varepsilon}} \Rightarrow N(\varepsilon) = \left[\sqrt{\frac{2}{\varepsilon}} \right].$

z) $\left| (-1)^n \cdot 0,999^n \right| = 0,999^n < \varepsilon \Leftrightarrow n \cdot \lg 0,999 < \lg \varepsilon$, bunda $\lg 0,999 < 0$ bo'lgani uchun

$$n > \frac{\lg \varepsilon}{\lg 0,999} \approx 2330 \cdot \lg \frac{1}{\varepsilon} \Rightarrow N(\varepsilon) = \left[2330 \cdot \lg \frac{1}{\varepsilon} \right] \blacktriangleright$$

43. Quyidagi

a) $x_n = (-1)^n \cdot n$, b) $x_n = 2^{\sqrt{n}}$, e) $x_n = \lg(\lg n)$, $n \geq 2$

ketma-ketliklar cheksiz katta ($\lim_{n \rightarrow \infty} x_n = \infty$) ekanligini isbotlang, ya'ni ixtiyoriy etarlicha katta $E > 0$ uchun $n > N$ bo'lganda $|x_n| > E$ tengsizlik bajariladigan $N(E)$ sonni ko'rsating.

◀ $E > 0$ - etarlicha katta son bo'lsin. U holda

b) $|x_n| = 2^{\sqrt{n}} > E \Leftrightarrow n > (\lg E)^2 \cdot (\lg 2)^{-2} \Rightarrow N(E) = \left[(\lg E)^2 \cdot (\lg 2)^{-2} \right]. \blacktriangleright$

44. $x_n = n^{(-1)^n}$ ($n = 1, 2, \dots$) ketma-ketlik chegaralanmagan va shu bilan birga $n \rightarrow \infty$ da cheksiz katta emasligini isbotlang.

◀ $\varepsilon > 0$ ixtiyoriy son bo'lsin. U holda $n = 2k$ va $k > \frac{\varepsilon}{2}$ bo'lganda

$|x_{2k}| = (2k)^{(-1)^{2k}} = 2k > \varepsilon$, ya'ni x_n chegaralanmagan. Vaholanki, $\varepsilon > 1$ va $n = 2k - 1$ da

$$|x_{2k-1}| = (2k-1)^{(-1)^{2k-1}} = \frac{1}{2k-1} < 1 < \varepsilon,$$

ya'ni cheksiz katta emas ►

45. Quyidagi tasdiqlarni tengsizliklar yordamida yozing:

a) $\lim_{n \rightarrow \infty} x_n = \infty$; b) $\lim_{n \rightarrow \infty} x_n = -\infty$; e) $\lim_{n \rightarrow \infty} x_n = +\infty$.

◀ a) $\lim_{n \rightarrow \infty} x_n = \infty \Leftrightarrow \forall \varepsilon > 0 \exists N(\varepsilon) \forall n > N(\varepsilon): |x_n| > \frac{1}{\varepsilon}$. ►

Quyidagi limitlarni aniqlang ($n \in \mathbb{N}$):

46. $\lim_{n \rightarrow \infty} \frac{10000n}{n^2 + 1}$.

Echimi. Limit ostidagi kasrning surat va maxrajini n^2 ga bo'lamiz va limitning xossalaridan foydalanib topamiz:

$$\lim_{n \rightarrow \infty} \frac{10000n}{n^2 + 1} = \lim_{n \rightarrow \infty} \frac{\frac{10000}{n}}{1 + \frac{1}{n^2}} = \frac{0}{1 + 0} = 0$$

48. $\lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^2} \sin n!}{n + 1}$.

Echimi. Limit ostidagi kasrning surat va maxrajini n^3 ga bo'lamiz. U holda $\sin n!$ chegaralanganligidan va limitning xossalaridan foydalanib topamiz:

$$\lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^2} \sin n!}{n + 1} = \lim_{n \rightarrow \infty} \frac{\sin n!}{n^3 + \frac{1}{\sqrt[3]{n^2}}} = 0$$

50. $\lim_{n \rightarrow \infty} \frac{1 + a + a^2 + \dots + a^n}{1 + b + b^2 + \dots + b^n}$, $|a| < 1$, $|b| < 1$.

Echimi. Limit ostidagi kasrning surat va maxrajidagi yig'indilarni topib (geometrik progressiya yig'indisi sifatida) va limitning xossalaridan foydalanib topamiz:

$$\lim_{n \rightarrow \infty} \frac{1 + a + a^2 + \dots + a^n}{1 + b + b^2 + \dots + b^n} = \lim_{n \rightarrow \infty} \frac{\frac{1 - a^{n+1}}{1 - a}}{\frac{1 - b^{n+1}}{1 - b}} = \frac{1 - b}{1 - a} \cdot \frac{1 - \lim_{n \rightarrow \infty} a^{n+1}}{1 - \lim_{n \rightarrow \infty} b^{n+1}} = \frac{1 - b}{1 - a}.$$

Bu erda $|a| < 1$ bo'lganda $\lim_{n \rightarrow \infty} a^n = 0$ ekanligidan foydalandik (49-misol echimiga qarang).

52. $\lim_{n \rightarrow \infty} \left| \frac{1}{n} - \frac{2}{n} + \frac{3}{n} - \dots + \frac{(-1)^{n-1} n}{n} \right|$.

Echimi. 1) $n = 2k$ da

$$\lim_{n \rightarrow \infty} \left| \frac{1}{n} - \frac{2}{n} + \frac{3}{n} - \dots + \frac{(-1)^{n-1} n}{n} \right| = \lim_{n \rightarrow \infty} \left| \frac{\overbrace{-1 + (-1) + \dots + (-1)}^{k \text{ marta}}}{n} \right| = \lim_{n \rightarrow \infty} \left| \frac{-\frac{n}{2}}{n} \right| = \frac{1}{2}$$

2) $n = 2k + 1$ da

$$\lim_{n \rightarrow \infty} \left| \frac{1}{n} - \frac{2}{n} + \frac{3}{n} - \dots + \frac{(-1)^{n-1} n}{n} \right| = \lim_{n \rightarrow \infty} \left| \frac{\overbrace{-1 + (-1) + \dots + (-1)}^{k \text{ ma}} + n}{n} \right| = \lim_{n \rightarrow \infty} \left| \frac{-\frac{n-1}{2} + n}{n} \right| = \lim_{n \rightarrow \infty} \frac{n+1}{2n} \rightarrow \frac{1}{2}.$$

Demak,

$$\lim_{n \rightarrow \infty} \left| \frac{1}{n} - \frac{2}{n} + \frac{3}{n} - \dots + \frac{(-1)^{n-1} n}{n} \right| = \frac{1}{2}.$$

$$53. \lim_{n \rightarrow \infty} \left(\frac{1^2}{n^3} + \frac{2^2}{n^3} + \dots + \frac{(n-1)^2}{n^3} \right).$$

Echimi. 2-misol va limitning xossalaridan foydalanamiz:

$$\begin{aligned} \lim_{n \rightarrow \infty} \left(\frac{1^2}{n^3} + \frac{2^2}{n^3} + \dots + \frac{(n-1)^2}{n^3} \right) &= \lim_{n \rightarrow \infty} \frac{1^2 + 2^2 + \dots + (n-1)^2}{n^3} = \\ &= \lim_{n \rightarrow \infty} \frac{(n-1)n(2n-1)}{6} = \lim_{n \rightarrow \infty} \frac{\left(1 - \frac{1}{n}\right) \cdot 1 \cdot \left(2 - \frac{1}{n}\right)}{6} = \frac{(1-0) \cdot (2-0)}{6} = \frac{2}{6} = \frac{1}{3}. \end{aligned}$$

$$55. \lim_{n \rightarrow \infty} \left(\frac{1}{2} + \frac{3}{2^2} + \frac{5}{2^3} + \dots + \frac{2n-1}{2^n} \right).$$

Echimi. Limit ostidagi ifodani $S_n = \frac{1}{2} + \frac{3}{2^2} + \frac{5}{2^3} + \dots + \frac{2n-1}{2^n}$ kabi belgilaymiz. Unda

$$\begin{aligned} S_n - \frac{1}{2} S_n &= \frac{1}{2} + \left(\frac{3}{2^2} - \frac{1}{2^2} \right) + \left(\frac{5}{2^3} - \frac{3}{2^3} \right) + \dots + \left(\frac{2n-1}{2^n} - \frac{2n-3}{2^n} \right) - \frac{2n-1}{2^{n+1}} = \\ &= \frac{1}{2} + \left(\frac{1}{2} + \frac{1}{2^2} + \dots + \frac{1}{2^{n-1}} \right) - \frac{2n-1}{2^{n+1}} \end{aligned}$$

Bundan S_n ni topamiz va limitni hisoblaymiz:

$$\begin{aligned} S_n &= 1 + 1 + \frac{1}{2} + \frac{1}{2^2} + \dots + \frac{1}{2^{n-2}} - \frac{2n-1}{2^n} = 1 + \frac{1 - \frac{1}{2^{n-1}}}{1 - \frac{1}{2}} - \frac{2n-1}{2^n} \\ \lim_{n \rightarrow \infty} S_n &= \lim_{n \rightarrow \infty} \left(1 + \frac{1 - \frac{1}{2^{n-1}}}{1 - \frac{1}{2}} + \frac{2n-1}{2^n} \right) = \lim_{n \rightarrow \infty} \left(1 + 2 - \frac{1}{2^{n-2}} - 2 \cdot \frac{n}{2^n} + \frac{1}{2^n} \right) = 3. \end{aligned}$$

Bu erda $\lim_{n \rightarrow \infty} \frac{n}{2^n} = 0$ dan foydalandik. Haqiqatan, $\varepsilon > 0$ ixtiyoriy son bo'lsin. U holda

$$\left| \frac{n}{2^n} \right| = \frac{n}{(1+1)^n} = \frac{n}{1+n+\frac{n(n-1)}{2}+\dots+1} < \frac{n}{\frac{n(n-1)}{2}} < \frac{2}{n-1} < \varepsilon \Leftrightarrow n > 1 + \frac{2}{\varepsilon} \Rightarrow N(\varepsilon) = \left[1 + \frac{2}{\varepsilon} \right].$$

Demak, $\lim_{n \rightarrow \infty} \frac{n}{2^n} = 0$.

$$57. \lim_{n \rightarrow \infty} \left(\sqrt{2} \cdot \sqrt[4]{2} \cdot \sqrt[8]{2} \cdot \dots \cdot \sqrt[2^n]{2} \right)$$

Echimi. Radikalning xossasi va geometrik progressiyaning yig'indisidan foydalanamiz:

$$\lim_{n \rightarrow \infty} (\sqrt{2} \cdot \sqrt[4]{2} \cdot \sqrt[8]{2} \cdot \dots \cdot \sqrt[2^n]{2}) = \lim_{n \rightarrow \infty} 2^{\frac{1}{2} + \frac{1}{4} + \dots + \frac{1}{2^n}} = \lim_{n \rightarrow \infty} 2^{1 - \frac{1}{2^n}} = \lim_{n \rightarrow \infty} \frac{2}{2^{\frac{1}{2^n}}}$$

Endi $n > 2$ da

$$2 = \left(2^{\frac{1}{2^n}}\right)^{2^n} = \left[1 + \left(2^{\frac{1}{2^n}} - 1\right)\right]^{2^n} > \left[1 + \left(2^{\frac{1}{2^n}} - 1\right)\right]^n = 1 + n\left(2^{\frac{1}{2^n}} - 1\right) + \dots + \left(2^{\frac{1}{2^n}} - 1\right)^n > n \cdot \left(2^{\frac{1}{2^n}} - 1\right)$$

Bundan $0 < 2^{\frac{1}{2^n}} - 1 < \frac{2}{n}$. Limitning xossasiga ko'ra $\lim_{n \rightarrow \infty} 2^{\frac{1}{2^n}} = 1$. Demak, $\lim_{n \rightarrow \infty} \frac{2}{2^{\frac{1}{2^n}}} = 2$.

4. Mavzuga doir testlar.

1. $\lim_{n \rightarrow \infty} \sqrt{n}(\sqrt{n+2} - \sqrt{n-3})$ ni hisoblang.

- A) $\frac{4}{3}$ B) $\frac{2}{5}$ *C) $\frac{5}{2}$ D) 3

2. $\lim_{n \rightarrow \infty} \left(\frac{1}{n^2} + \frac{2}{n^2} + \dots + \frac{n-1}{n^2}\right) = ?$

- A) $\frac{1}{2}$ *B) 1 C) $\frac{3}{2}$ D) $\frac{1}{3}$

3. $\lim_{n \rightarrow \infty} (1 + 2 + 3 + \dots + n) \frac{1}{n}$ limitni hisoblang.

- A) 1 B) 0 C) $\frac{1}{2}$ *D) ∞

4. $\lim_{n \rightarrow \infty} \frac{2n^2 - 1}{3 - n^2}$ limitni hisoblang.

- A) $-\frac{1}{3}$ B) 0 C) $\frac{2}{3}$ *D) -2

5. $\lim_{n \rightarrow \infty} \frac{n^2 - n}{1 - n}$ limitni hisoblang.

- A) $\frac{1}{2}$ B) 0 *C) ∞ D) 1

6. $\lim_{n \rightarrow \infty} \frac{(-1)^n}{2n + 5}$ limitni hisoblang.

- *A) 0 B) $\frac{1}{2}$ C) ∞ D) $\frac{1}{7}$

7. $\lim_{n \rightarrow \infty} \sqrt[n]{a} = ?$ ($a > 0$)

- A) 0 B) a *S) 1 D) \neq E) ∞

8. $\lim_{n \rightarrow \infty} \sqrt[n]{n} = ?$

- A) 0 B) 2 *S) 1 D) 3 E) ∞

9. $\lim_{n \rightarrow \infty} \frac{n}{2^n} = ?$

- *A) 0 B) $\frac{1}{2}$ S) -1 D) 1 E) ∞

10. Agar $\{x_n\}$ ketma-ketlik uchun quyidagi shart bajarilsa, ya`ni

$$\exists a : \forall \varepsilon > 0 \exists n_0 \in N \forall n > n_0 \quad |x_n - a| < \varepsilon, \text{ u holda } \dots$$

- A) Ketma-ketlik uzoqlashuvchi *B) Ketma-ketlik yaqinlashuvchi
C) Yaqinlashuvchi ham , uzoqlashuvchi ham emas D) To`g`ri javob yo`q

11. Agar $\{x_n\}$ ketma-ketlik uchun quyidagi shart bajarilsa, ya`ni

$$\forall a : \exists \varepsilon > 0 \forall n_0 \in N \exists n > n_0 \quad |x_n - a| \geq \varepsilon, \text{ u holda } \dots$$

- *A) Ketma-ketlik uzoqlashuvchi B) Ketma-ketlik yaqinlashuvchi
C) Yaqinlashuvchi ham , uzoqlashuvchi ham emas D) To`g`ri javob yo`q

12. Agar $\{x_n\}$ yaqinlashuvchi bo`lsa, uning limiti ...

- A) 2 ta B) Mavjud emas *C) Yagona D) Cheksiz

5. Mustaqil ish topshiriqlari.

1. 42 a), b); 43 a), b); 45 b), b).[3]
2. 47, 49, 51, 54, 56.[3]
3. 3.1. punkt misollari: 1-30.[4]

Adabiyotlar.

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